

Article **Characteristics of Downward and Upward Longwave Radiation at Athalassa, an Inland Location of the Island of Cyprus**

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Abstract: In this study, two years of hourly longwave downward and upward irradiance measurements at Athalassa, an inland location, are used to analyze and compare them. A detailed quality control process was followed according to the suggested tests proposed by the Baseline Surface Radiation Network (BSRN) group. The criteria involved are based on physically possible, extremely rare and climatological limits. Furthermore, comparison tests were also applied between the two longwave components as well as with air and ground surface temperatures. Additionally, time consistency and persistency tests were applied. All the suspect data were excluded from the analysis. The data showed that the frequency distribution of downward longwave irradiances follows a normal distribution function, while the upward longwave follows an almost normal distribution but with a long positive tail. The annual mean daily downward longwave irradiation is 27.3 MJ m⁻² and the annual mean daily upward longwave irradiation is 37.8 MJ m⁻². The net longwave irradiation is always negative ranging from -5.9 to -12.1 MJ/m². Various models were tested to estimate daylight and all day downward and upward longwave irradiances under clear-sky and all-sky conditions. For the comparison of measured and estimated values the root-mean-square errors and linear regression correlations have been used. The results of this comparison showed that Idso's and Brunt's models perform well, and they can be used to estimate downward longwave irradiance under clear-sky conditions. Furthermore, both models were extended to estimate the daylight downward longwave irradiance under all-sky conditions by taking into account the ratio of global to the clear-sky global solar irradiance. In this case, the RMSE of the local calibrated coefficients scheme of Idso's model was 30.6 W m⁻², while Brunt's model showed slightly lower value (29.0 W m⁻²).

Keywords: downward longwave radiation; upward longwave radiation; net longwave radiation; quality control; statistical analysis; modeling

1. Introduction

The radiation budget at the ground surface is important to understand the climate system and its variability. Net radiation (R_n) is the sum of the net shortwave radiation (0.3– 3.0 μ m) (R_{ns}) and the net longwave radiation (0.3–100 μ m) (R_{nl}). The net shortwave is the difference between the incoming global solar radiation (G) and the reflected radiation (R) from the ground, while the net longwave radiation is the difference between the downward (L_{dn}) and upward (L_{up}) radiation components. Therefore, the net radiation (R_n) is generally defined as the difference between incoming and outgoing radiation of both short and long wavelengths and it is expressed as follows [\[1\]](#page-27-0):

$$
R_n = R_{ns} + R_{nl} = G(1 - \rho_g) + L_{dn} - L_{up}
$$
\n(1)

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where ρ_g is the surface albedo (fraction of Reflected radiation to Global radiation). Net radiation represents the effective energy provided by sun to heat soil and air as well as to evaporate soil surface water.

The downward longwave radiation originates from gases present in the atmosphere such as water vapor, carbon dioxide, and ozone. About 90% of the downward longwave radiation at the ground surface comes from the first 800–1600 m of the atmosphere [\[2\]](#page-27-1). Therefore, the water vapor pressure and the air temperature are closely related to *Ldn*. The role of clouds is also significant for the amount of the emitted downward irradiance [\[3,](#page-27-2)[4\]](#page-27-3). On the other hand, the upward longwave radiation depends on the emittance/absorptance properties of the material at the ground surface and its temperature and is always higher than the downward irradiance. Therefore, the longwave radiation balance is normally negative. The knowledge of this radiation is important for agricultural meteorology and building heating/cooling systems, energy budget studies, frost forecasting and environmental applications [\[5–](#page-27-4)[7\]](#page-28-0). Furthermore, the downward longwave radiation has shown a remarkable increase during the process of global warming [\[8\]](#page-28-1).

The longwave radiation components can be estimated by four different methods [\[9\]](#page-28-2), i.e., (1) direct measurements by pyrgeometers in meteorological stations, which is the most accurate method; (2) simple physical or empirical models which are the most popular and use mainly temperature and relative humidity and follow the Stefan–Boltzmann equation with recalibration of the coefficients under local conditions; (3) radiative transfer models which are data demanding and use meteorological observations from different layers of the atmosphere; and (4) through satellite observations where their accuracy needs to be improved. As outlined earlier, most of these empirical equations follow the Stefan–Boltzmann law:

$$
F = \varepsilon * \sigma * T_s^4 \tag{2}
$$

where *F* is the longwave radiation flux emitted by any surface which depends on the absolute surface temperature T_s and on the longwave emittance *ε*. The constant *σ* is the Stefan– Boltzmann constant ($\sigma = 5.66697 * 10^{-8}$ Wm⁻²K⁻⁴). The total emissivity can be estimated from clear-sky effective emissivity (ε_c) and the emissivity which is modulated by clouds (*εcl*). Dozens of parameterization formulas have been developed in which clear-sky effective emissivity is calculated as a function of the screen-level air temperature (*Ta*) and water vapor pressure (e), since about half the longwave radiation comes from the lowest 100 m of the atmosphere [\[1\]](#page-27-0). Details about the formulae for estimating emissivity are given by various authors [\[10–](#page-28-3)[12\]](#page-28-4). Prata [\[13\]](#page-28-5) found that the precipitable water content was much better to represent the effective emissivity of the atmosphere than the water vapor pressure. Other authors [\[14](#page-28-6)[,15\]](#page-28-7) have extended the calculations of emissivity by adopting the effect of land use.

Alados-Arboledas [\[16\]](#page-28-8) has estimated the effect of clouds on the longwave irradiance. The downward longwave radiation can be increased up to 34% with an overcast sky of low clouds [\[17\]](#page-28-9). Maghrabi et al. [\[18\]](#page-28-10) have studied the influence of atmospheric water content, temperature, and aerosol optical depth on downward longwave radiation in arid conditions. Crawford and Duchon [\[12\]](#page-28-4) proposed a cloud fraction for all-sky conditions, which was defined as the ratio of the measured solar radiation to the clear-sky radiation (k_c) . Other authors used the clearness index (k_t) , which is defined as the ratio of the measured solar radiation to the extraterrestrial solar radiation [\[7](#page-28-0)[,19\]](#page-28-11). Therefore, the cloud modification factor (*clf'* or *clf*) can be estimated as follows:

$$
clf' = 1 - k_c \text{ or } clf = 1 - k_t \tag{3}
$$

The determination of the daytime downward longwave radiation is estimated in all cases under clear-sky and all-sky conditions [\[4](#page-27-3)[,11](#page-28-12)[,20](#page-28-13)[–23\]](#page-28-14). However, Chang and Zhang [\[7\]](#page-28-0) have proposed a downward longwave model based on air temperature and relative humidity under all-sky conditions which are classified into four cases: All-day, nighttime, and daytime with and without considering the cloud modification factor.

A lot of publications appeared in the literature concerning the shortwave radiation components measured at Athalassa [\[24–](#page-28-15)[28\]](#page-28-16), and Petrakis et al. [\[29\]](#page-28-17) have presented the "Typical Meteorological Year" for Nicosia (Cyprus). More recently, Kalogirou et al. [\[30\]](#page-28-18) presented an assessment of the solar radiation climate at two sites in Cyprus one at Athalassa an inland location and the second one at Larnaca a coastal location, based on measurements of about two years. Furthermore, Pashiardis et al. [\[31\]](#page-28-19) have analyzed the direct, diffuse, and global short-wave irradiation using three years of data. The characteristics of the longwave downward and upward irradiance at two sites in Cyprus were also presented by Pashiardis et al. [\[9\]](#page-28-2). The paper has also evaluated various empirical models under clear-sky and all-sky conditions.

The current study covers two years of measurements (2016–2017) of various short and longwave radiation components and has four objectives. Firstly, the longwave data were undergone an extensive quality control process based on tests proposed by the Baseline Surface Radiation Network (BSRN). The tests include globally physical possible, extremely rare and climatological configurable limits as well as global cross-comparisons for the surface longwave radiation measurements [\[32\]](#page-28-20). Furthermore, consistency and persistency tests were applied to improve the validity of the data. Secondly, the data were statistically analyzed to reveal the characteristics of longwave radiation on a monthly and hourly basis. Furthermore, we implement simple empirical models which were developed in a previous study under clear and all-sky conditions using local calibrated coefficients [\[9\]](#page-28-2). Finally, the net longwave radiation is calculated from the difference of downward and upward longwave irradiances and estimated from other models based on air temperature, relative humidity and global solar radiation.

2. Measurements and Quality Control Processes

The radiation data on which this study is based are obtained from Athalassa meteorological station which is an inland plain location (Figure [1\)](#page-2-0). The coordinates of the station are shown in Table [1.](#page-3-0)

Figure 1. Map of Cyprus showing the location of Athalassa radiometric station. **Figure 1.** Map of Cyprus showing the location of Athalassa radiometric station.

Table 1. Site parameters for the Athalassa meteorological station.

The climate of Athalassa is typical Mediterranean with mild winters (mean seasonal air temperature of about 10.5 ◦C) and warm and dry summers (mean seasonal air temperature of about 29.5 \degree C). The annual rainfall is about 320 mm. Rainfall is recorded mainly between October and March. The average annual sunshine duration is 3332 h. The annual average daily global radiation is 18.5 MJ m⁻² and the average yearly cumulative global irradiation is about 6763 MJ m−² . Statistical analysis showed that clear and partially cloudy days exceed the value of 80% of the year [\[30\]](#page-28-18).

CG1 pyrgeometers obtained from Kipp and Zonen were used to measure the longwave radiation. All the sensors are factory calibrated, in accordance with the World Radiometric Reference (WRR) [\[33\]](#page-28-21). About 9% of the upward longwave irradiance data values are missing, while the percentage of the downward longwave irradiance which is missing is about 25%. The missing data are caused either from problematic functioning of the CG1 pyrgeometers or from problems related to the data logger system. Long missing data for both longwave irradiances are observed in the year 2017. Details about the quality control procedures for the shortwave solar radiation measurements can be found in [\[34\]](#page-28-22).

Longwave Radiation Quality Control

The process of quality control for the longwave radiation is based on range tests which were suggested by the Baseline Surface Radiation Network (BSRN) group. BSRN has proposed globally physical possible, extremely rare, and climatological configurable limits as well as global cross-comparisons for the surface longwave radiation measurements [\[32\]](#page-28-20) (Table [2\)](#page-3-1).

Table 2. Physically possible and extremely rare global limits recommended by BSRN and user configurable climatological limits, as well as global cross-comparisons based on air temperature (*Ta*) (in Kelvin) and between the two longwave variables. *σ* is the Stefan–Boltzman constant = 5.67×10^{-8} Wm⁻² K⁻⁴.

The "physically possible" tests detect extremely large errors in the radiation data. The radiation data falling in the intervals defined by the range between 40 and 700 W/m^2 for downward longwave irradiance and between 40 and 900 W/m^2 for the upward longwave irradiance are considered "physically possible". The data set passed the suggested physical limits.

The "extremely rare" limits are narrower than those of the "physically possible" limits, since they usually occur over very short time periods under very extreme conditions.

Therefore, "good quality" is assumed to be inside the "extremely rare" limits. Figure [2](#page-4-0) shows that downward longwave irradiances (*Ldn*) are within the specified limits. However, about 0.4% of data of the upward longwave irradiances (L_{up}) have values slightly above $700 \ \text{W}/\text{m}^2$, with a maximum value of $738 \ \text{W}/\text{m}^2$ (Figure [2\)](#page-4-0).

Figure 2. Marginal plot of the hourly downward and upward longwave irradiances at Athalassa. The scatter plot also shows the boxplots of the two variables. Reference lines are the extremely rare and the climatological limits (1st and 2nd level) for the upward and downward longwave irradiances as given by Table 2. level) for the upward and downward longwave irradiances as given by Table [2.](#page-3-1)

The suggested climatological limits are based on data obtained from the Great Plains in the United States. The limits are classified in two levels. The 1st level has the "smallest" testing limits, while those referred as "2nd level" give the second lower limits. Downward longwave irradiances passed all the given criteria, while the upward longwave irradiances 4 0.4 0.4 0.4 m₂ and the downward longwave values are as high as the outgoing longwave noted that some of the downward longwave values are as high as the outgoing longwave layers above the planetary boundary layer [18]. showed slightly higher values than the suggested upper limits (Table [2\)](#page-3-1). It has to be radiation. These values may be attributed to high aerosol optical depth values from warm

longwave irradiances and their relationships with air temperature data (T_a) at the screen level. The formulae involved with temperature relationships have the following ranges: The global cross comparison tests are referred to various comparisons between the two

$$
0.4 * \sigma * T_a^4 < L_{dn} < \sigma * T_a^4 + 25W \, \text{m}^{-2} \tag{4}
$$

$$
\sigma * (T_a - 15K)^4 < L_{up} < \sigma * (T_a + 25K)^4 \tag{5}
$$

The lower limit of the comparison test of Equation (4) is formulated in such a way that the value of the effective atmospheric emittance, defined by $\varepsilon_a = L_{dn}/\sigma * T_a^4$ is not possible to be less than 0.4. On the other hand, a longwave component greater than a black-body emission at surface temperature, is also considered impossible. The comparisons between the two longwave components are also shown in Table 2.

The results of these comparisons are shown in Figure [2.](#page-4-0) The marginal plot shows also the variability of the two variables through their boxplots. The boxplot of the downward irradiance is almost symmetrical around the mean value indicating that this variable follows an approximately normal frequency distribution function. On the other hand, the boxplot of the upward longwave irradiance shows a large number of outliers towards the upper tail of the boxplot. As indicated earlier, a small number (0.4%) of the data points of the upward longwave irradiance are above the extremely rare limits (700 W m−²). However, it has to be noted that the climatological limits are based on observations measured in the Great Plains of United States, where the climatological conditions may be different from those in Athalassa. Furthermore, it has to be noted that air temperatures have increased by more than 0.5 ℃ per decade in the recent years since 1980 due to the climate change process in the region of Eastern Mediterranean and Middle East [\[35](#page-28-23)[–37\]](#page-29-0). Therefore, it is expected that both longwave components will have higher values in the future.

The effect of air temperature at the screen level on both longwave irradiances is illustrated in Figure [3.](#page-5-0) For example, for a range of air temperatures between 15 and 20 °C, the upward longwave irradiance is around 400 W/m^2 , while the downward longwave irradiance ranges mainly between 250 and 350 W/m² . Generally, *Ldn* ranges between 200 and 450 W/m² during the day, while during the night when temperatures are lower, L_{dn} has slightly narrower upper limits (200 to 400 W/m²). On the other hand, L_{up} ranges mainly between 300 to 700 W/m² during the day, while during the night it has also narrower upper limits (300 to 550 W/m^2). upper limits (300 to 550 W/m²).
As shown in Figure [4](#page-6-0) the longwave data points, estimated by Equations (4) and (5) are

450 Shown in Figure 4 the longwave data points, estimated by Equations (4) and (5) are within the ranges as described by the said equations. However, the downward irradiance at Athalassa during the period May–November 2017, showed unreasonable very low values
and they did not pass the said criteria. Therefore, 4128 bourly values were excluded from and they did not pass the said criteria. Therefore, 4128 hourly values were excluded from the statistical analysis due to instability of the pyrgeometer. The total number of missing records for upward irradiances is only 1421 as shown by Table [3.](#page-7-0)

Figure 3. The effect of air temperature at the screen level on both the downward and upward longwave irradiances.

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Figure 4. (a) Downward and (b) Upward longwave irradiance testing versus air temperature (Global cross-comparisons,
— Equations (4) and (5)). Green represents the upper limit and blue the lower limit.

Variable	Unit	N	Mean	StDev	Min	Q_1	Median	Q_3	Max
G	W/m ²	7834	403.1	302.69	0.0	113.3	384.6	659.9	1020.7
R	W/m^2	8135	91.0	58.89	0.0	39.4	89.8	136.9	227.8
R_{ns}	W/m ²	7029	355.9	230.23	7.1	145.1	344.3	551.5	850.1
L_{dn}	W/m^2	13,414	316.5	50.22	185.5	278.2	315.4	351.7	469.6
L_{up}	W/m^2	16,121	436.9	92.04	292.7	367.0	414.8	476.1	738.0
R_{nl}	W/m ²	13,412	-105.4	57.51	-293.5	-133.6	-93.4	-71.3	3.6
T_a	$^{\circ}C$	17.457	20.1	8.65	-1.9	13.4	20.0	26.5	44.2
T_g	$^{\circ}C$	17,424	17.9	10.13	-6.2	10.0	17.5	24.8	46.2
RH	$\%$	17,460	60.9	21.42	10.0	43.0	63.0	79.0	99.0
\mathfrak{e}	hPa	17,457	14.2	5.58	3.2	10.0	13.1	17.4	31.4

Table 3. Annual basic statistics of the hourly global (*G*), reflected (R), net shortwave (*Rns*), downward (*Ldn*), upward (*Lup*) and net longwave (*Rnl*) irradiances in W m−² , air temperature at the screen level (*Ta*), air temperature near the ground surface (*Tg*), relative humidity (*RH*), and actual vapor pressure (*e*) for the period of two years (2016–2017).

The extreme rare limits can be also obtained by the range of values defined by the limits of 3 times of the standard deviation interval from the mean value. Values outside these thresholds should be considered as extreme values. Using the data set, the intervals for the downward and upward irradiances calculated by the mean ± 3**StDev*, have the following ranges which are closed to the extremely rare limits: L_{dn} : 166–467 W m⁻², L_{up} : 161–713 W m⁻².

Regarding the range test of the net longwave irradiance (*Rnl*), Table [3](#page-7-0) shows that the data point values are within the suggested limits shown in Table [2.](#page-3-1) The annual mean value of R_{nl} is -105 W m^{-2} .

Another quality control test is the step test. This test is based on time consistency which compares the difference between successive measurements. If the difference exceeds an allowed value, then both observations are flagged as suspects. For example, Estevez et al. [\[38\]](#page-29-1) proposed the following values for different variables: for hourly global irradiance they proposed the value of 555 W m⁻² and for hourly air temperature the value of 7 °C, while for relative humidity the value of 45%. The data set confirms the limits of the above variables. For the longwave irradiances there is no information in the literature for the difference of two successive measurements. According to the available data set the rate of changes of downward and upward irradiances are <50 W m⁻² and <65 W m⁻², respectively.

Finally, the persistency test was applied to check the variability of the measurements. When a sensor fails, it will often report a constant value. There is no evidence of such constant values of the given variables through the time series plots (Figure [5\)](#page-8-0). The graph shows that long missing data for both the downward and upward longwave irradiances are observed in the year 2017. The higher values of both variables are recorded during the summer period, while the lower during the winter period, since both of them are related to the air or ground surface temperatures. The variability of upward irradiance is higher than that of downward irradiance.

Figure 5. Time series plots of the (a) hourly downward and upward longwave irradiances (b) hourly global shortwave irradiances and (**c**) hourly air temperatures (*Ta*) at screen level at Athalassa. irradiances and (**c**) hourly air temperatures (*Ta*) at screen level at Athalassa.

3. Results and Discussion 3. Results and Discussion

3.1. Diurnal Variation of Longwave Irradiances

The daily variation of the hourly downward (L_{dn}) , upward (L_{up}) , net longwave irradiances, ground surface temperature and the atmospheric emissivity are shown in Figure [6.](#page-11-0) The curves follow a sinusoidal pattern (similar to air temperature) with the maximum around 14:00 local time and the minimum around 06:00. The highest mean hourly values of *L*_{*dn*} are obtained in July (435 W m^{−2}) and the lowest values in February (265 W m^{−2}). The highest mean hourly values of L_{up} are obtained again in July (692 W m^{−2}) highest mean hourly values of *Lup* are obtained again in July (692 W m−2) and the lowest

and the lowest values in January (330 W m^{−2}). Since *L*_{*up*} is always higher than *L*_{*dn*}, the mean hourly net longwave irradiance (*Rnl* = *Ldn* − *Lup*) is always negative, ranging from -47 W m⁻² in the morning to -265 W m⁻² in the midday. The lower negative values of the hourly *Rnl* during midday are associated with the higher ground surface temperatures which are recorded at the station (Figure [6c](#page-11-0),d). Similar variation of the above variables was also obtained for the period 2013–2015 [\[9\]](#page-28-2). The average hourly emissivity (ε_a) is 0.77 ± 0.08 and shows slightly lower values during the winter months and around 0.8 during the summer months when the weather conditions are more stable (Figure 6e). longwave irradiance ($R_{nl} = L_{dn} - L_{up}$) is always negative, ranging from l t/ W m^{−2} in the morning to −265 W m^{−2} in the midday. The lower negative values of the hourly *R_{at}* during midday are associated with the higher ground surface tempe

Figure 6. Diurnal variation of the (a) downward (L_{dn}), (b) upward (L_{up}), (c) net longwave irradiances (R_{nl}) (d) ground surface temperatures (T_g) and (**e**) Annual variability of the hourly estimated effective air emissivity (ε_a).

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Figure 6. *Conts.*

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Figure 6. *Conts.*

3.2. Seasonal Variation of Longwave Irradiances

3.2. Seasonal Variation of Longwave Irradiances The monthly statistics of the longwave and shortwave irradiances and their associated standard deviations and extreme values are presented in Table [4.](#page-12-0) The monthly means of all the radiation components are also shown in Figure [7.](#page-12-1) The monthly means of *L*_{*dn*} of all the radiation components are also shown in Figure 7. The monthly means of *dn L* range between 280 and 387 W/m² with the lowest values in the winter months and the highest during the summer months. Similar variation is observed for the upward longwave irradiance ranging from 355 to 529 W/m². The net longwave irradiance is always negative, ranging from −68 in the winter months to −140 W/m² in the summer months. The lower negative values during the summer months are associated with the higher ground surface temperatures. The mean values of global irradiance are comparable to the upward longwave irradiances (*L*_{*up*}). However, the maximum of global irradiances may exceed the value of 1000 W/m², while L_{up} reached the value of 738 W/m². Furthermore, the monthly variability of longwave irradiances expressed by their standard deviation is much the main and respective variable $\frac{1}{2}$ variable $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ is the standard deviation in $\frac{1}{2}$ irradiances range mainly between 50 and 130 W/m² with the highest occurring in the $\frac{1}{2}$ summer months. The net shortwave irradiance is positive throughout the year, ranging from 195 to 444 W/m². However, the net allwave irradiances are positive during the first 10 months of the year and slightly below zero during the last two months of the year (November and December). lower than the respective values of global irradiance. The mean values of the reflected

Rad.	Stat.	Var.	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec	All
LW		L_{dn}	286	280	290	304	327	367	387	387	359	339	300	295	316
LW		L_{up}	355	372	390	432	457	507	529	516	487	450	391	363	437
LW		R_{nl}	-69	-92	-100	-128	-130	-140	-140	-132	-126	-111	-91	-68	-105
SW	Mean	G	236	310	386	446	442	494	498	487	439	366	300	206	403
SW		\boldsymbol{R}	49	71	85	92	89	112	127	119	108	94	65	48	91
SW		R_{ns}	231	288	336	399	393	444	429	395	375	324	249	195	356
AW		R_n	25	32	64	85	96	199	227	193	64	37	-29	-29	75
LW		L_{dn}	$45\,$	41	35	37	36	35	30	31	32	25	32	38	50
LW		L_{up}	32	45	49	71	73	92	95	88	80	70	49	29	92
LW		R_{nl}	45	40	44	57	59	64	67	63	60	55	43	38	58
SW	Std	G	196	236	276	314	317	338	337	313	290	260	210	173	303
SW		\boldsymbol{R}	34	44	51	51	53	59	65	64	62	51	43	37	59
SW		R_{ns}	152	177	215	245	249	250	245	236	213	185	158	133	230
AW		R_n	131	158	196	221	222	273	276	258	186	154	110	98	212
LW		L_{dn}	185	186	217	229	243	303	333	333	294	284	241	222	185
LW		L_{up}	293	298	323	326	359	384	404	404	376	352	313	308	293
LW		R_{nl}	-179	-190	-240	-279	-282	-284	-293	-293	-274	-256	-205	-156	-293
SW	Min	\boldsymbol{G}	$\mathbf{0}$	θ	0	0	0	$\mathbf{0}$	$\overline{0}$	$\overline{0}$	θ	$\overline{0}$	$\overline{0}$	$\overline{0}$	$\mathbf{0}$
SW		\boldsymbol{R}	2	2	$\overline{2}$	$\overline{2}$	$\overline{2}$	$\overline{0}$	8	1	$\boldsymbol{0}$	$\overline{4}$	θ	$\overline{0}$	$\boldsymbol{0}$
SW		R_{ns}	14	8	9	10	10	15	18	7	8	17	9	9	$\overline{7}$
AW		R_n	-146	-145	-147	-147	-153	-114	-116	-113	-134	-122	-192	-156	-192
LW		L_{dn}	413	397	383	409	423	470	463	464	454	423	404	397	470
LW		L_{up}	488	532	559	635	648	726	738	713	684	629	534	454	738
LW		R_{nl}	4°	4	-4	-1	-4	-9	-45	-31	-10	-1	-1	-1	4
SW	Max	G	672	792	915	994	995	1021	986	999	887	805	685	551	1021
SW		\boldsymbol{R}	137	167	194	217	198	212	223	228	214	177	144	150	228
SW		R_{ns}	563	662	755	850	841	829	779	783	709	628	540	455	850
AW		R_n	416	550	562	636	630	794	771	783	478	394	371	407	794

Table 4. Monthly statistics of longwave (LW) and shortwave (SW) irradiances and their associated standard deviations (Std) and extreme values in W/m^2 .

onthly mean values of the short and longwave irradiances including the net allwave irradiances in irradiances in W/m2. Figure 7. Monthly mean values of the short and longwave irradiances including the net allwave irradiances in W/m² .

3.3. Frequency Distribution of Longwave Irradiances 3.3. Frequency Distribution of Longwave Irradiances

Figure 7. Monthly mean values of the short and longwave irradiances including the net allwave

Figure 8 shows the [a](#page-13-0)nnual frequency distributions of the hourly downward and upward irradiances. As can be seen *Ldn* irradiances follow the normal distribution function, ward irradiances. As can be seen *Ldn* irradiances follow the normal distribution function, while *Lup* follows an almost normal distribution but with a long positive tail. The annual while *Lup* follows an almost normal distribution but with a long positive tail. The annual cumulative density function curves (*CDF*) of the two variables are presented in Figure [9.](#page-13-1) cumulative density function curves (*CDF*) of the two variables are presented in Figure 9. As indicated from the graph, in 75% of the irradiances, *Ldn* at Athalassa are lower than 350 W m−² . For the upward longwave irradiance (*Lup*), for the same probability, the irradiances are lower than 480 W m⁻². As indicated from the graph, in 75% of the irradiances, L_{dn} at Athalassa are 350 W m−2. For the upward longwave irradiance (*L_{up}*), for the same probability

 $\frac{1}{2}$ a. $\frac{1}{2}$ and $\frac{1}{2}$ and $\frac{1}{2}$ with the annual frequency distributions of the two variables at Atl variables at Athalassa. **Figure 8.** Marginal plot of the hourly *Ldn* and *Lup* with the annual frequency distributions of the two variables at Athalassa.

Figure 9. Cumulative density function (*CDF*) for *Ldn* and *Lup* at Athalassa. **Figure 9.** Cumulative density function (*CDF*) for *Ldn* and *Lup* at Athalassa.

The monthly variation of both variables is shown in Figure [10.](#page-14-0) The outliers are prepresented with an asterisk and as seen, significant number of outliers of *Ldn* is observed in June and during the period of September to November. In the case of L_{up} , outliers are In yane and during the period of September to November. In the case of *Lup*, outliers are observed at the beginning of the year (in the first three months) and towards the end of the year (in the last two months). year (in the last two months). served at the beginning of the year (in the first three months) and towards the end of the

Figure 10. Monthly boxplots of (a) downward (L_{dn}) and (b) upward (L_{up}) longwave irradiances at Athalassa.

3.4. Statistical Relationships of Hourly Values

The variables illustrated in Figure [8,](#page-13-0) can be expressed by quadratic equations. However, the coefficient of determination is relatively low:

$$
L_{dn} = -10.01 + 1.058 * L_{up} - 0.0006 * L_{up}^2, R^2 = 0.57
$$
 (6)

The quadratic equations of the relationships between the hourly longwave irradiances with air (T_a) and ground surface temperatures (T_g) are shown below:

$$
L_{dn} = 251.9 + 2.035 * T_a + 0.068 * T_a^2, R^2 = 0.62
$$
 (7)

$$
L_{dn} = 258.3 + 3.195 \times T_g + 0.021 \times T_g^2, R^2 = 0.60
$$
 (8)

$$
L_{up} = 325.1 + 0.152 \times T_a + 0.227 \times T_a^2, R^2 = 0.88
$$
\n(9)

$$
L_{up} = 329.2 + 1.969 \times T_g + 0.172 \times T_g^2, R^2 = 0.96 \tag{10}
$$

It is evident that *Lup* has strong relationships with both air and ground surface temperatures. The coefficient of determination of the relationship of L_{up} and T_g is closed to 1.

3.5. Daily Data

Figure [11](#page-15-0) shows the temporal evolution of the daily downward and upward longwave irradiation. As can be seen, during the winter and spring season a strong variability occurs. The maximum daily value of L_{dn} is 35.2 MJ m⁻² while the respective minimum value is 17.4 MJ m⁻². The maximum value of L_{up} is 48.3 MJ m⁻² and the minimum value is 26.3 MJ m⁻².

Figure 11. Daily downward and upward longwave irradiation at Athalassa, during the period 2016–2017. **Figure 11.** Daily downward and upward longwave irradiation at Athalassa, during the period 2016–2017.

The monthly statistics of daily downward and upward longwave irradiation is shown in Table [5,](#page-16-0) which presents the following statistical parameters: number of observations (N), arithmetic mean (Mean), standard deviation (StDev), coefficient of variation in percent (CV(%)), minimum (Min), the first and third quartiles (Q1 and Q3), and median and maximum (Max). Generally, the median values are close to the mean values. The variability of *Lup* is lower than *Ldn*, since its coefficient of variation (CV%) ranges from 2% to 5%. *Ldn* has higher variability during the winter and spring months.

The monthly mean daily values of all radiation components are plotted in Figure [12.](#page-16-1) Longwave irradiation shows the highest mean daily values comparing to the other shortwave radiation components. *Lup* has the highest mean daily values from all the radiation components. The higher values of both longwave irradiation are observed during the summer months due to higher air and ground surface temperatures. As a result, the net longwave irradiation is always negative ranging from -5.9 to -12.1 MJ/m². The net longwave irradiation represents the radiative cooling potential. On the other hand, the net shortwave irradiation (R_{ns}) ranges from 6.6 to 22.4 MJ/m². Therefore, the net daily irradiation is positive ranging from 1.3 to 10.5 MJ/m² . The pattern of *Rⁿ* follows the same as the *Rns*, i.e., higher values during the summer season. The variability of the net short, long and allwave radiation components is presented in Figure [13.](#page-17-0) The highest variability is observed during the winter and spring months as it is indicated by the length of the boxplots.

Figure [14](#page-17-1) shows the CDF curves of the daily downward and upward longwave irradiation. As can be seen in both cases in 60% of the days the L_{dn} is lower than 28.3 MJ m⁻² and L_{up} is lower than 40 MJ m⁻².

L_{dn} (MJ/m ²)								
$\mathbf N$	Mean	StDev	$CV(\%)$	Min	Q ₁	Median	Q ₃	Max
58	24.7	3.3	13.4	17.4	22.5	24.8	26.8	31.2
56	24.2	3.0	12.3	17.7	22.2	24.4	26.5	29.5
62	25.0	2.3	9.0	20.9	22.9	24.9	26.6	31.1
60	26.3	2.3	8.7	22.0	24.5	26.8	27.9	32.1
53	28.3	2.1	7.5	24.8	26.4	28.1	29.7	34.1
30	31.7	1.7	5.5	29.2	30.3	31.2	33.0	35.0
31	33.4	0.7	2.0	32.5	32.9	33.4	33.9	35.1
31	33.4	0.9	2.8	31.7	32.5	33.3	34.2	35.2
30	31.0	1.8	5.8	27.3	29.9	31.4	32.5	33.4
31	29.3	1.1	3.6	27.3	28.5	29.3	29.9	31.4
51	25.8	2.0	7.7	22.9	24.6	25.4	27.4	32.0
61	25.4	2.5	9.8	20.2	23.7	25.1	26.8	31.4
554	27.3	3.8	13.8	17.4	24.7	27.1	29.9	35.2
${\bf N}$	Mean	StDev	$CV(\%)$	Min	Q1	Median	Q ₃	Max
					29.8		31.6	33.2
56	32.1	1.8	5.5	28.6	31.0	31.9	33.1	35.7
62	33.7							
		1.4	4.2	30.9	32.7	33.8	34.6	36.7
60	37.3	2.1	5.5	32.8	35.5	37.7	39.1	40.8
53	39.5	1.8	4.5	35.6	37.7	39.8	41.1	42.1
58	43.8	1.8	4.2	39.2	42.6	43.3	45.3	47.5
62	45.7	0.9	1.9	43.7	45.1	45.8	46.2	48.3
62	44.6	$0.8\,$	1.9	43.0	43.9	44.7	45.1	46.1
53	42.0	1.3	3.1	39.1	40.8	42.3	42.8	44.2
31	38.9	1.2	3.1	37.0	37.9	38.6	40.0	40.9
51	33.8	1.5	4.3	31.6	32.4	33.9	34.8	36.6
61	31.4	1.0	3.3	28.5	30.6	31.4	32.2	33.5
	L_{up} (MJ/m ²) 58	30.6	1.3	$4.1\,$	26.3		30.6	

Table 5. Statistics of daily downward and upward longwave irradiation (MJ m⁻²) at Athalassa.

Figure 12. Monthly mean daily longwave and shortwave irradiation components. **Figure 12.** Monthly mean daily longwave and shortwave irradiation components.

Figure 13. Boxplots of the daily (a) net shortwave (R_{ns}) , (b) net longwave (R_{nl}) , and (c) net allwave irradiation (R_n) (MJ/m²). diation. As can be seen in both cases in both cases in 60% of the days the annual continuous (1.40%)

Figure 14. Cumulative density function (CDF) of the daily downward (L_{dn}) and upward (L_{up}) longwave irradiation (MJ m⁻²) at Athalassa. at Athalassa.

3.6. Relationships with Daily Data

A linear relationship was established between the daily downward and upward longwave irradiation (MJ m⁻²):

$$
L_{dnd} = 5.581 + 0.597 * L_{upd}, \ R^2 = 0.66 \tag{11}
$$

There is also a strong correlation between the daily longwave upward irradiation and the daily shortwave reflected irradiation since both are depended on the properties of the soil (Figure [15\)](#page-18-0):

$$
L_{upd} = 28.88 + 1.270 * R_d + 0.204 * R_d^2, R^2 = 0.79 \tag{12}
$$

Figure 15. Quadratic relationship between the daily longwave upward irradiation (L_{upd}) and the daily shortwave reflected $irradiation (R_d).$

3.7. Parameterizing Daytime Longwave Downward Radiation 3.7. Parameterizing Daytime Longwave Downward Radiation

3.7.1. Clear-Sky Conditions 3.7.1. Clear-Sky Conditions

Since the downward longwave radiation is greatly affected by air temperature and/or Since the downward longwave radiation is greatly affected by air temperature and/or va-por pressure at the screen level parameterizing was based on these variables. Pashiardis et al. [\[9\]](#page-28-2) have estimated daytime longwave downward irradiance under clear sky conditions using five different models. For this purpose, hourly temperature and relative humidity data were used to estimate *L*_{*dn*}. The classification of the clear-sky conditions was based on the value of the clearness index k_t , which is defined as the hourly ratio of the measured global solar irradiance to the value of extraterrestrial horizontal solar irradiance ($k_t = G/G_0$). Then, the sky can be considered as clear when ($k_t \geq 0.65$), as partly cloudy when (0.35 $\leq k_t < 0.65$), and cloudy when ($k_t < 0.35$) [39] $(k_t \leq 0.35)$ [\[39\]](#page-29-2).

The best performance of the test models was obtained with Idso [\[40\]](#page-29-3) and Brunt's [\[41\]](#page-29-4) models using local calibrated coefficients based on data measurements covering the period 2013-2014 (training dataset). The equations involved in the calculations of the longwave

downward irradiance under clear sky conditions (*Ldnc*) with local calibrated coefficients have the following form:

$$
L_{dnc} = [0.71 + 4.09 * 10^{-5} e * \exp(1500/T_a)] * \sigma * T_a^4 \text{ (Idso model)}
$$
 (13)

$$
L_{dnc} = (0.62 + 0.046 * e^{0.5}) * \sigma * T_a^4 \text{(Brunt model)} \tag{14}
$$

where, *e* is the actual vapor pressure in hPa, *T^a* is the air temperature at screen level in Kelvin and σ is the Stefan–Boltzman constant. The above models were tested with the current data set hourly values. The performance of the above models was based on the root-mean-square error (RMSE), and the correlation between the estimated (*Eⁱ*) and the measured irradiance values (*Mⁱ*). The RMSE has the following form:

RMSE =
$$
\left[\frac{1}{n}\sum_{i=1}^{n} (E_i - M_i)^2\right]^{0.5}
$$
 (15)

where *n* is the number of data pairs. The results of the evaluation of both models for the clear sky conditions are shown in Table [6.](#page-19-0) The Table shows that the slope of the lines and the coefficients of determinations are close to one for both clear sky models. However, Brunt's model shows slightly better performance with respect to Idso's model, since it has slightly lower RMSE compared to Idso's model.

Table 6. Comparison of statistical estimators of the two calibrated daylight downward longwave irradiance models under (a) clear-sky and (b) all-sky conditions at Athalassa using the current data set (2016–2017).

Sky Conditions	Model	Variable	Slope	R^2	RMSE $(W/m2)$
Clear sky	Idso	L_{ndc}	1.017	0.997	21.819
	Brunt	L_{ndc}	1.019	0.997	19.347
All-sky	Idso L_{ndc}	L_{nd}	1.070	0.992	30.597
	Brunt L_{ndc}	L_{nd}	1.061	0.993	29,009

3.7.2. Estimation of Downward Irradiance under All-Sky Conditions

Bilbao and De Miguel [\[42\]](#page-29-5) proposed the following equation for the estimation of the daylight downward longwave irradiance under all-sky conditions (*Ldn*):

$$
L_{dn} = L_{dnc} [1 + p(1 - G/G_c)^q]
$$
 (16)

where *Ldnc* is the daylight downward longwave irradiance under clear-sky conditions (Equations (14) and (15)), *G/Gc* is the ratio of the measured global solar horizontal irradiance to clear-sky global horizontal irradiance, and *p* and *q* are empirical coefficients. The above equation was selected because the experimental station proposed by the researches is an inland one with a latitude of about $41°$ N i.e., closed to our site of measurements. Clear-sky hourly horizontal irradiance was estimated from the following equation obtained from Haurwitz [\[43\]](#page-29-6):

$$
G_c = 1098 * \cos(\theta_z) * \exp(-0.057 / \cos(\theta_z))
$$
\n(17)

where θ_z is the solar zenith angle.

The calibration of the coefficients *p* and *q* of Equation (16) was based on the training data set (2013–2014) and its evaluation on the independent validation data set (2015). The final estimated local coefficients of *p* and *q* had the following values [\[9\]](#page-28-2):

p = 0.212 and *q* = 1.608 for the Idso model, and

p = 0.238 and *q* = 1.613 for the Brunt model.

Similar values of *p* coefficients were obtained in Valladolid (Spain) [\[42\]](#page-29-5), but the *q* coefficients at Athalassa are almost twice higher than those in Spain.

Using the current data set, and the coefficients reported earlier, the results of this exercise are presented in Table [6.](#page-19-0) As can be seen the slopes and the coefficients of determination are close to unity for both models for clear-sky conditions. On the other hand, both models showed slightly higher RMSE values than those obtained with clear conditions. Similar results were obtained by Bilbao and De Miguel [\[42\]](#page-29-5) in Valladolid, Spain. The fitted line of the estimated versus the measured hourly daylight downward longwave irradiances under all-sky conditions, using the Idso's and Brunt's clear-sky models are shown in Figure [16.](#page-20-0) As seen, the data points are within the 95% prediction intervals. Additionally, the coefficients of determination are very close to each other, i.e., 71% and 72%, respectively, for each model.

Figure 16. Comparison of measured and estimated hourly daylight downward longwave irradiances under all-sky conditions 2017). for the calibrated coefficients of (**a**) Idso's and (**b**) Brunt's models at Athalassa using the current dataset (2016–2017).

3.7.3. Parameterizing Longwave Downward Radiation for the All-Day Time Interval

The previous section described the estimation of *Ldn* during the daylight hours. The longwave radiation during daytime is necessary for the energy balance applications, while that during the nighttime is more favourable for the building passive cooling systems [\[4\]](#page-27-3). Chang and Zhang [\[7\]](#page-28-0) have proposed an empirical equation to calculate (*Ldn*) for the all-day, nighttime and daytime intervals. The proposed equation has the following form:

$$
L_{dn} = \sigma * (T_a)^4 * (a * \ln(e/T_a) + b * RH + c)
$$
\n(18)

where T_a is the air temperature in Kelvin, *e* is the actual vapor pressure in hPa and *RH* is the relative humidity in percentage; *a*, *b*, and *c* are empirical coefficients. The proposed equation was selected because it is based on routine measurements of a meteorological station. For the all-day time interval, the original coefficients proposed by the authors have the following values: $a = 0.08$, $b = 0.0011$, and $c = 1.029$. The coefficients of daytime and nighttime intervals showed almost similar values with those for the all-day time interval. Based on a training data set which covers the period of 2013–2015, the locally calibrated coefficients have been estimated giving the following values: $a = 0.039$, $b = 0.0007$ and $c = 0.884$ [\[9\]](#page-28-2). The performance of the model showed a coefficient of determination of R^2 = 0.74 and a RMSE = 22.95 W/m². Figure [17](#page-21-0) shows the comparison of the estimated L_{dn} for the all-day time interval and the measured values of *Ldn* for the data set of the period 2016–2017. The R^2 is about 0.68 and the standard deviation of the residuals (*S*) is 21.869 (Figure [17\)](#page-21-0). Almost all the data points are within the 95% prediction intervals.

Figure 17. Comparison of estimated and measured L_{dn} for the all day time interval for the data set of the period 2016–2017.

3.8. Longwave Upward Radiation Parameterization

The estimation of the upward emitted longwave irradiance from the ground surface is based on the Stefan–Boltzman equation:

$$
L_{up} = \varepsilon_{\lg} * \sigma * T_g^4 \tag{19}
$$

The longwave emittance of natural ground surfaces, ε_{lg} , is typically around 0.96 [\[44\]](#page-29-7). T_g is the ground surface temperature given in Kelvin. In a sunny weather, T_g is higher than the screen air temperature (T_a) , but on clear winter nights it is below T_a . Figure [18a](#page-22-0) shows the relationship between the estimated longwave irradiance and the measured one using Equation (19). The graph shows a strong correlation between the two variables ($R^2 = 0.93$), although a quadratic equation could give even higher correlation ($R^2 = 0.96$).

Figure 18. (a). Comparison of measured and estimated hourly upward longwave irradiances for the whole day using Equation (19). (**b**). Comparison of measured and estimated hourly daylight upward longwave irradiances for the calibrated $\mathcal{L}_{\mathcal{A}}$ have also estimated daytime upward is also estimated day to estimate as a as a same upward in Dognieux and Lemoine model at Athalassa using the data set 2016–2017.

Dognieux and Lemoine [\[45\]](#page-29-8) have also estimated daytime upward irradiance as a function of ground surface temperature, global solar radiation (*G*) in W m−² and the ground albedo (ρ_{φ}) which is defined as the ratio of the Reflected solar irradiance to Global solar irradiance:

$$
L_{up} = \sigma * [0.995 * T_g + 0.023 * (1 - \rho_g) * G]^4
$$
\n(20)

The above equation was used for the estimation of the daytime upward irradiance of the European Solar Radiation Atlas and therefore it was tested under Cyprus environmental conditions. The yearly average value of the ground albedo at Athalassa is 0.214. In the current study, the hourly values of the albedo are used for the estimation of the upward longwave irradiance. The coefficients of Equation (20) were locally calibrated [\[9\]](#page-28-2). The original coefficients are very close to the calibrated ones. Figure [18b](#page-22-0) shows the relationship between the estimated daytime longwave irradiance and the measured one. The figure indicates that there is also a strong correlation between the two variables (R^2 = 0.942).

3.9. Net Longwave Radiation

The hourly net longwave irradiance, as indicated earlier, can be calculated from the respective difference of the downward and upward longwave irradiances. The hourly evolution of the calculated *Rnl* irradiances are shown in Figure [6c](#page-11-0), while Table [5](#page-16-0) and Figure [12](#page-16-1) show the monthly daily net longwave radiation. Equation (16) is applied to estimate downward irradiance values by using the coefficients obtained from the best performance Brunt model, whereas Equation (20) is used to estimate the upward longwave irradiance using the local calibrated coefficients. The scatterplot of the relationship between the estimated and calculated R_{nl} is shown in Figure [19a](#page-24-0). As indicated in the graph, the dispersions of the points are close to the fitted line with $R^2 = 0.815$.

The net all-day downward longwave irradiance can be estimated from the difference of Equation (18) and the upward longwave irradiance estimated by Equation (19). The scatterplot of the relationship between the estimated and measured *Rnl* is shown in Figure [19b](#page-24-0). In this case, the coefficient of determination is $R^2 = 0.683$. The low coefficient of determination is attributed to the weak relationship obtained from the downward irradiance. Therefore, the prediction of *Rnl* is better for the daytime rather the all-day interval.

Allen et al. [\[46\]](#page-29-9) proposed an empirical equation to estimate the daily net longwave radiation (R_{nl}) given by

$$
R_{nl} = \sigma_{SB} * T_a^4 * (0.34 - 0.14 * e^{0.5}) * (1.35 * G/G_c - 0.35)
$$
 (21)

where $\sigma_{SB}=4.903*10^{-9}$ MJ m⁻² K⁻⁴ d⁻¹ (Stefan–Boltzman constant), T_a is the mean daily air temperature in K, *e* is the mean daily vapor pressure in kPa, *G* is the measured daily global solar radiation in MJ m^{−2}, and G_c is the calculated daily clear-sky radiation (MJ m^{−2}). The above equation is used by WMO for the estimation of the reference evapotranspiration. Using all the available data, the above formula overestimates the net longwave radiation during the most months except the summer period (Figure [20\)](#page-25-0).

Figure 19. Comparison of measured and estimated hourly net longwave irradiances using the local calibrated coefficients at Athalassa for the period 2016–2017 (validation dataset), during (**a**) daytime and (**b**) all day intervals.

Figure 20. Comparison of the estimated Equation (21) and the measured daily net longwave radiation, at Athalassa.

4. Conclusions 4. Conclusions

Two years of hourly longwave downward and upward irradiance measurements for an inland location are used in the current study. Firstly, the data were undergone an extensive quality control process which was based on tests proposed by the BSRN group. These tests refer to physically possible limits, extremely rare, and climatological limits as These tests refer to physically possible limits, extremely rare, and climatological limits as well as comparison tests between the two longwave components and with air and ground surface temperatures. The upward irradiances showed slightly higher values than the climatological limits as suggested by the BSRN group. The slight excess (about 0.4% of data points) of the climatological limits of the upward irradiance could be attributed probably points) of the climatological limits of the upward irradiance could be attributed probably to the higher temperatures which prevail at this location. Therefore, all the upward to the higher temperatures which prevail at this location. Therefore, all the upward longwave irradiance data were kept in the analysis. On the other hand, the downward longwave irradiance data were kept in the analysis. On the other hand, the downward irradiance showed unreasonable very low values during the period May–November 2017 and they did not pass the comparison criteria with air temperature. Therefore, 4128 hourly values of downward longwave irradiance were excluded from the statistical analysis due irradiance showed unreasonable very low values during the period May–November 2017
and they did not pass the comparison criteria with air temperature. Therefore, 4128 hourly
values of downward longwave irradiance were excl to instability of the pyrgeometer. Regarding to the time consistency test which assess the difference between successive measurements the available data set showed that the rate of changes between successive hours of the downward and upward irradiances are <50 W m⁻² and <65 W m⁻², respectively.

transpiration. Using all the available data, the above formula overestimates the net

The second objective of this study refers to the statistical analysis of both hourly and daily values of the longwave radiation including their frequency distribution. As shown, a strong variability is observed during the winter and spring season. The maximum daily value of L_{dn} is 35.2 MJ m⁻² while the respective minimum value is 17.4 MJ m⁻². The maximum daily value of *Lup* is 48.3 MJ m−² and the minimum value is 26.3 MJ m−² . The annual mean daily downward longwave irradiation is 27.3 MJ m⁻². On the other hand, the annual mean daily upward longwave irradiation is 37.8 MJ m⁻². The higher air and ground surface temperatures are responsible for the higher values of upward longwave radiation at this site (inland), especially during the summer period at which *Lup* has the highest mean daily values from all the radiation components. As a result, the net longwave irradiation at Athalassa is always

negative ranging from -5.9 to -12.1 MJ/m², which represents the radiative cooling potential. On the other hand, the net shortwave irradiation (R_{ns}) ranges between 6.6 and 22.4 MJ/m². Therefore, the net daily irradiation is positive ranging from 1.3 to 10.5 MJ/m². The pattern of R_n follows the same as the R_{nl} , i.e., higher values during the summer season. Regarding the frequency distribution of *Ldn* irradiances the data showed that it follows a normal distribution function, while *Lup* follows an almost normal distribution but with a long positive tail. Since air temperatures are higher due to climate change process, we expect that both longwave components would be increased in the future.

A final objective was the estimation and evaluation of the performance of various models in estimating the downward and upward longwave irradiances under clear and allsky conditions during daytime or all the time of the day. For the case of clear sky conditions, the Idso's and Brunt's models were selected which showed the best performance among five models. For this purpose, local calibrated coefficients were estimated based on a training data set of the period 2013–2014 [\[9\]](#page-28-2). Implementing the data set for the period 2016–2017 showed that Brunt's model showed slightly better results than Idso's model, since RMSE was lower than that Idso's model.

The estimated longwave radiation during all-day time interval is based on air temperature and relative humidity measurements according to the model proposed by Chang and Zhang [\[7\]](#page-28-0). Based on a training data set which covers the period of 2013–2015, the local calibrated coefficients have the following values: $a = 0.039$, $b = 0.0007$, and $c = 0.884$ [\[9\]](#page-28-2). The performance of the model showed a relatively strong correlation with a coefficient of determination of $R^2 = 0.74$ and a RMSE = 22.95 W/m².

The estimation of the upward longwave irradiance is more successful since it depends mainly on ground surface temperature and the properties of the soil and it can be estimated by the Stefan–Boltzman equation. The estimated and measured upward irradiances showed a strong correlation between the two variables (R^2 = 0.93). A second model was tested for the estimation of the upward irradiance during daytime which was proposed by Dognieux and Lemoine [\[45\]](#page-29-8). The model again showed a strong correlation between the estimated and measured values ($R^2 = 0.942$).

The results of the study can be used for the estimation of the radiative cooling and the forecasting of the surface ground and air temperatures. Radiative cooling can reduce the energy consumption for building cooling in summer which is important in saving energy in very hot environments.

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Abbreviations

- *a* Coefficient of the parameterization models
b Coefficient of the parameterization models
- *b* Coefficient of the parameterization models
- *c* Coefficient of the parameterization models
- *CDF* Cumulative density function
- *CV* Coefficient of variation (%)
- *clf* Cloud modification factor $(1-k_t)$
clf Cloud modification factor $(1-k_c)$
- *clf*⁰ Cloud modification factor (1-*kc*)
- *e* Screen level water vapour pressure (hPa)
- *es* Saturated screen level water vapour pressure (hPa)
- E_i Estimated longwave irradiance [W m⁻²]
- *F* Longwave radiation flux [W m^{−2}]

- G_d Global solar irradiation [MJ m⁻²]
- G_0 Extraterrestrial irradiance [W m⁻²]
- G_{0d} Daily extraterrestrial irradiation (ETR) [MJ m⁻²]
- G_c Clear-sky global solar irradiance [W m⁻²]
- G_d Daily global irradiation [MJ m⁻²]
- *Gsc* Solar constant [1367 W m−²]
- *k*_{*c*} Clear sky hourly clearness index (*G*/*G*_{*c*}) K_T Daily clearness index (*G*_{*d*}/*G*_{0*d*})
- K_T Daily clearness index (*G_d*/*G*_{0*d*})
- k_t Hourly clearness index (*G*/*G*₀)
- *^Ldn* Downward longwave irradiance [W m−²]
- *L*_{dnc} Downward longwave irradiance under clear-sky conditions [W m^{−2}]
- *Lup* Upward longwave irradiance [W m−²]
- *LW* Longwave radiation
- M_i Measured longwave irradiance [W m⁻²]
- *N* Non missing observations
- *p* Coefficient of the parameterization models
- *q* Coefficient of the parameterization models
- *Q1* First Quartile
- *Q3* Third Quartile
- R^2 ² Coefficient of determination
- *R* Reflected irradiance [W m^{−2}]
- R_d Daily reflected radiation [MJ m⁻²]
- *RH* Relative humidity (%)
R_{nsd} Daily Net shortwave is
- *R*_{*nsd*} Daily Net shortwave irradiation [MJ m^{−2}]
- R_{ns} Net shortwave irradiance [W m⁻²]
- *R*_{*nl*} Net longwave irradiance [W m^{−2}]
- R_n Net all wave irradiance [W m⁻²]
- RMSE Root Mean Square Error
- *S* Standard deviation of residuals
- StDev Standard deviation (Std)
- SW Shortwave radiation
- *Ta*($\rm ^{\circ}C$) Air temperature at screen level ($\rm ^{\circ}C$), $T_a(K) = 273.16 + T_a(\rm ^{\circ}C)$
- *T*_{*g*}(°C) $\rm{^{\circ}C}$ Ground surface temperature ($\rm{^{\circ}C}$), $T_g(K) = 273.16 + T_g(\rm{^{\circ}C})$
- $\overline{T_s}$ ^oC) $\rm{°C}$) Surface temperature ($\rm{°C}$), $T_s(K) = 273.16 + T_s(\rm{°C})$
- Greek
- *ε* Longwave emittance
- *ε^α* Atmospheric longwave emittance
- *εc* Clear sky effective longwave emittance
- *εcl* Cloudy sky effective longwave emittance
- *εlg* Ground surface longwave emittance
- *θz* Solar zenith angle (SZA) [degrees]
- ρ_g Albedo (*R*/*G*)
- σ_{SB} Stefan–Boltzman constant (5.66697*10⁻⁸ W m⁻²K⁻⁴)

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