

A Study on the Dynamic Behavior of Wheel-Type Train Propelled by Superconducting Linear Synchronous Motor

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Abstract

This paper deals with a study on the dynamic behavior of 600 km/h wheel-type train propelled by superconducting linear synchronous motor (LSM). This train is of a traditional wheel-on-rail type with traction motors on wheel-bogies. However, for the 600 km/h speed, on the both sides of each vehicle, superconducting LSMs are attached and the ground coils are installed on the guideway. In this case, the guideway irregularities act as disturbance to the vehicle causing deterioration of ride comfort. And besides thrust force, the normal force could be created in superconducting LSM control, which influences vehicle dynamics during running. In this study, to examine the effect of guideway irregularity and normal force on dynamic behavior of proposed train, the vehicle dynamic model is driven and frequency analysis is performed through simulation. The simulation results show that the lateral directional acceleration is mainly influential to ride comfort; however this could be reduced effectively by electromagnetic damping force from linear generator. It is also shown that the normal force effect from superconducting LSM control is limited even though the attractive normal force acts favorably to ride comfort.

Keywords

High Speed Railway, Superconducting Linear Synchronous Motor, Dynamic Behavior

1. Introduction

Technology competitions for increasing the speed of rail transportation constantly become fierce around the world. Conventional wheel-type railways such as TGV, ICE, Shinkansen, etc. are being commercialized with maximum speed of 300 km/h and now under development for over 500 km/h speed. Meanwhile, as an alternative for high speed rail transportation, the maglev using linear synchronous motor (LSM) is also being commercialized in Shanghai China with 430 km/h as maximum speed [\[1\].](#page-9-0) And Japan has built a construction plan of Tokyo-Nagoya route by maglev until 2027 and conducted the performance test in 42.8 km test line [\[2\]](#page-9-1) [\[3\].](#page-9-2)

Despite the superiority in high speed, the drawback such as interoperability problem that maglev could not interoperated with the existing wheel-on-rail track is the main obstacle for maglev commercialization [\[4\].](#page-9-3) To resolve this problem while aiming at the high speed, compared with the 300 km/h level wheel type railway and 400 km/h level maglev, the new concept of high speed railway aiming at 600 km/h level is recently introduced by C. Y. Lee [\[5\].](#page-9-4) In [\[5\],](#page-9-4) author proposed the dual-mode propulsion system propelled by traction motors in low speed and superconducting LSM in high speed. As shown in **[Figure 1](#page-2-0)**, by adopting the traditional wheel type rail, the interoperability problem with existing railroad could be resolved and by installing superconducting electromagnets on vehicle sides and ground LSM coils on the exclusive high speed line, the powerful thrust force could be achieved.

In superconducting LSM propulsion, since the thrust force is produced from interactive force between electromagnets on vehicle and LSM coils on guideway, the irregularities of guideway cause deterioration of ride comfort [\[6\].](#page-9-5) Since the precise construction of guideway requires excessive amount of cost, active vibration control based on vehicle dynamic analysis should be considered to improve the ride comfort. And in superconducting LSM propulsion control, the normal directional force in respect of thrust direction could be created by adjusting the magnetic field angle [\[5\],](#page-9-4) so the normal force effect on the vehicle dynamic behavior is also needed to be analyzed.

In this study, as a model for dynamic analysis, the Korea high speed wheel type train (KTX) attaching superconducting electromagnets on vehicle sides is assumed. Based on the proposed model, the computation model and mathematical equations including external disturbance are established. Then, through the simulations, system dynamic behavior according to the guideway irregularities and normal forces is analyzed and the ride comfort improvement method is suggested.

2. Vehicle Dynamic Model

2.1. Configuration of Proposed Vehicle Model

The configuration of vehicle model for dynamic analysis is shown in **[Figure 2](#page-2-1)**. The forehead motor car of KTX with two wheel bogies is adopted as main body and it is assumed that superconducting electromagnets are attached on sides without shape modification of main body. Therefore, the major vehicle characteristics are determined by wheel-bogies whose detail components are described in **[Figure 3](#page-2-2)** [7]. Based on this, the vehicle dynamic model for vertical, lateral and rolling direction could be established like **[Figure 4](#page-3-0)**. The descriptions of symbols in this model are as follows:

- m_1 , m_2 : masses of bogie and car body
- I_1 , I_2 : moment of inertial of bogie and car body
- $k_{\scriptscriptstyle m}$, $k_{\scriptscriptstyle n}$: spring constants of bogie in lateral and vertical direction
- k_{xy} , k_{yz} : spring constants of car body in lateral and vertical direction
- c_{p_y} , c_{p_z} : damping constants of bogie in lateral and vertical direction
- $c_{\rm sv}$, $c_{\rm sv}$: damping constants of car body in lateral and vertical direction
- h_{k0} , h_{k1} , h_{k2} : lateral spring attachment height
- h_{c1} , h_{c2} ; lateral damper attachment height
- b_{k1} , b_{k2} : half of the lateral distance between vertical springs
- b_{c1} , b_{c2} : half of the lateral distance between vertical dampers
- y_1 , y_2 : lateral displacement
- $\varnothing_1, \varnothing_2$: rolling angular displacement
- z_1 , z_2 : vertical displacement
- y_0 , z_0 : guideway irregularity of lateral and vertical direction

The characteristic values of dynamic model are described in **[Table 1](#page-3-1)** [\[7\].](#page-9-6) In here, the subscript "1(p)" means "bogie(primary)" and "2(s)" means "car body(secondary)". And the subscript "a" and "b" means different com-

Figure 3. Bogie system of KTX forehead motor ca[r \[7\].](#page-9-6)

Figure 4. Dynamic model of proposed vehicle.

ponents with same function.

2.2. Dynamic Equation for Vertical Direction

Based on the dynamic model achieved previously, the dynamic equations for vertical direction could be expressed as follows:

Bogie vertical motion

$$
m_1 \ddot{z}_1 + (c_{pza} + c_{sza} + c_{szb}) \dot{z}_1 - (c_{sza} + c_{szb}) \dot{z}_2 + (k_{pza} + k_{pzb} + k_{sza} + k_{szb}) z_1 - (k_{sza} + k_{szb}) z_2
$$

= $c_{pz} \dot{z}_0 + (k_{pza} + k_{pzb}) z_0$ (1)

Car body vertical motion

$$
m_2\ddot{z}_2 - (c_{sza} + c_{szb})\dot{z}_1 + (c_{sza} + c_{szb})\dot{z}_2 - (k_{sza} + k_{szb})z_1 + (k_{sza} + k_{szb})z_2 = 0
$$
\n(2)

If we set the state variable like

$$
\boldsymbol{x} = \begin{bmatrix} z_1, \dot{z}_1, z_2, \dot{z}_2 \end{bmatrix}^\mathrm{T}
$$
 (3)

and the state space equation like

$$
\dot{x} = A x + B z_0 , \qquad (4)
$$

then, the system matrix *A* could be expressed like

$$
A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ -\frac{(k_{pza} + k_{pzb} + k_{sza} + k_{szb})}{m_1} - \frac{(c_{pza} + c_{sza})}{m_1} & \frac{(k_{sza} + k_{szb})}{m_1} & \frac{c_{sza}}{m_1} \\ 0 & 0 & 0 & 1 \\ \frac{(k_{sza} + k_{szb})}{m_2} & \frac{(c_{sza} + c_{szb})}{m_2} - \frac{(k_{sza} + k_{szb})}{m_2} - \frac{(c_{sza} + c_{szb})}{m_2} \end{bmatrix}
$$
(5)

And the external input term, Bz_0 can be express like

$$
\boldsymbol{B}z_{0} = \begin{bmatrix} 0 \\ \frac{c_{pza}}{m_{1}} \dot{z}_{0} + \frac{(k_{pza} + k_{pzb})}{m_{1}} z_{0} \\ 0 \\ 0 \end{bmatrix} .
$$
 (6)

If input is sinusoidal such as $z_0 = H \sin(\omega t)$, the second element in Equation (6) can be re-expressed as follows:

$$
\frac{c_{pza}}{m_1}\dot{z}_0 + \frac{(k_{pza} + k_{pzb})}{m_1}z_0 = \frac{c_{pza}}{m_1}H\omega\cos(\omega t) + \frac{(k_{pza} + k_{pzb})}{m_1}H\sin(\omega t) = \Omega\sin(\omega t - \alpha) \tag{7}
$$

where

$$
\Omega = \frac{H}{m_1} \sqrt{(c_{pza})^2 + (k_{pza} + k_{pzb})^2}, \quad \alpha = \tan^{-1} \left(-\frac{k_{pza} + k_{pzb}}{c_{pza}} \right).
$$

Then, Equation (6) can be simplified like

$$
\boldsymbol{B}z_{0} = \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \end{bmatrix} \Omega \sin(\omega t - \alpha). \tag{8}
$$

2.3. Dynamic Equation for Lateral and Rolling Direction

To achieve the dynamic equations for lateral and rolling direction of proposed system, the similar procedure to previous section could be applied. However, in this case, since the energy balanced equation about momentum should be constructed, the distance between components position and mass center described in **[Table 1](#page-3-1)** should be considered. And it is assumed that the lateral disturbance, y_0 originated from guideway irregularity acts on the mass center of bogie for simplicity. The dynamic equation for lateral and rolling direction could be expressed as follows:

Bogie lateral motion

$$
m_1 \ddot{y}_1 + (k_{pya} + k_{pyb}) y_1 + c_{py} \dot{y}_1 - (k_{sya} + k_{syb}) (y_2 - y_1) - (c_{sya} + c_{syb}) (\dot{y}_2 - \dot{y}_1) + (k_{pya} h_{k0a} + k_{pyb} h_{k0b}) \varnothing_1 + c_{py} h_{c0} \dot{\varnothing}_1 - k_{sya} (h_{k2a} \varnothing_2 + h_{k1a} \varnothing_1) - k_{syb} (h_{k2b} \varnothing_2 + h_{k1b} \varnothing_1) - c_{sya} (h_{c2a} \dot{\varnothing}_2 + h_{c1a} \dot{\varnothing}_1) - c_{syb} (h_{c2b} \dot{\varnothing}_2 + h_{c1b} \dot{\varnothing}_1) = (k_{pya} + k_{pyb} + k_{sya} + k_{syb}) y_0
$$
\n(9)

Car body lateral motion

$$
m_2 \ddot{y}_2 + (k_{sys} + k_{sys}) (y_2 - y_1) + (c_{sys} + c_{sys}) (\dot{y}_2 - \dot{y}_1) + k_{sys} (h_{k2a} \mathcal{O}_2 + h_{k1a} \mathcal{O}_1) + k_{sys} (h_{k2b} \mathcal{O}_2 + h_{klb} \mathcal{O}_1)
$$

+
$$
c_{sys} (h_{c2a} \dot{\mathcal{O}}_2 + h_{c1a} \dot{\mathcal{O}}_1) + c_{sys} (h_{c2b} \dot{\mathcal{O}}_2 + h_{c1b} \dot{\mathcal{O}}_1) = 0
$$
 (10)

Bogie rolling motion

$$
I_{1}\ddot{\varnothing}_{1} + (k_{pya}h_{k0a} + k_{pyb}h_{k0b})y_{1} + c_{py}h_{co}\dot{y}_{1} + (k_{sya}h_{k1a} + k_{syb}h_{k1b})(y_{2} - y_{1}) + (c_{sya}h_{c1a} + c_{syb}h_{c1b})(\dot{y}_{2} - \dot{y}_{1}) + (k_{pya}b_{k0a}^{2} + k_{pyb}b_{k0b}^{2})\varnothing_{1} + c_{py}h_{co}^{2}\dot{\varnothing} + k_{sya}h_{k1a}(h_{k2a}\varnothing_{2} + h_{k1a}\varnothing_{1}) + k_{syb}h_{k1b}(h_{k2b}\varnothing_{2} + h_{k1b}\varnothing_{1}) + c_{sya}h_{c1a}(h_{c2a}\dot{\varnothing}_{2} + h_{c2b}\dot{\varnothing}_{1}) + c_{syb}h_{c1b}(h_{c2b}\dot{\varnothing}_{2} + h_{c1b}\dot{\varnothing}_{1}) + (k_{pza}b_{k1a}^{2} + k_{pzb}b_{k1b}^{2})\varnothing_{1} + (c_{pza}b_{c1a}^{2} + c_{pzb}b_{c1b}^{2})\varnothing_{1} - k_{sza}(b_{k2a}^{2}\varnothing_{2} - b_{k2a}^{2}\varnothing_{1}) - k_{szb}(b_{k2b}^{2}\varnothing_{2} - b_{k2b}^{2}\varnothing_{1}) - c_{sza}(b_{c2a}^{2}\dot{\varnothing}_{2} - b_{c2a}^{2}\dot{\varnothing}_{1}) - c_{szb}(b_{c2b}^{2}\dot{\varnothing}_{2} - b_{c2b}^{2}\dot{\varnothing}_{1}) = 0
$$
\n(11)

Car body rolling motion

$$
I_{2}\ddot{\varnothing}_{2} + (k_{sys}h_{k2a} + k_{sys}h_{k2b})(y_{2} - y_{1}) + (c_{sys}h_{c2a} + c_{sys}h_{c21b})(\dot{y}_{2} - \dot{y}_{1}) + k_{sys}h_{k2a}(h_{k2a}\varnothing_{2} + h_{k1a}\varnothing_{1})
$$

+ $k_{sys}h_{k2b}(h_{k2b}\varnothing_{2} + h_{k1b}\varnothing_{1}) + c_{sys}h_{c2a}(h_{c2a}\dot{\varnothing}_{2} + h_{c1a}\dot{\varnothing}_{1}) + c_{sys}h_{c2b}(h_{c2b}\dot{\varnothing}_{2} + h_{c1b}\dot{\varnothing}_{1}) + k_{s2a}(b_{k2a}^{2}\varnothing_{2} - b_{k2a}^{2}\varnothing_{1})$ (12)
+ $k_{s2b}(b_{k2b}^{2}\varnothing_{2} - b_{k2b}^{2}\varnothing_{1}) + c_{s2a}(b_{c2a}^{2}\dot{\varnothing}_{2} - b_{c2a}^{2}\dot{\varnothing}_{1}) + c_{s2b}(b_{c2b}^{2}\dot{\varnothing}_{2} - b_{c2b}^{2}\dot{\varnothing}_{1}) = 0$

If we set the state variable like

$$
\boldsymbol{x} = \left[y_1, \dot{y}_1, y_2, \dot{y}_2, \mathcal{O}_1, \dot{\mathcal{O}}_1, \mathcal{O}_2, \dot{\mathcal{O}}_2 \right]^T
$$
\n(13)

and the state space equation like

$$
\dot{x} = A x + B z_0 , \qquad (14)
$$

then, the elements of matrix *A* and *B* could be achieved in a similar way described in previous section.

3. Simulation Results

Based on dynamic equations driven in previous section, the simulation regarding ride comfort by using the frequency response analysis in vertical, lateral and rolling direction was performed. For the vertical directional simulation, as an input z_0 , a sine wave with a magnitude 10 mm and 100 m wavelength is used [\[8\].](#page-9-7) And as a lateral and rolling direction disturbance input y_0 , a 1 mm magnitude and 100 m wavelength sine wave is used [\[6\].](#page-9-5) In both cases, the travel speed of train is assumed as 500 km/h.

3.1. Ride Comfort Analysis

The frequency response of car body in vertical direction is shown in **[Figure 5](#page-6-0)**. The peak value with $1.2 \text{ m/s}^2/\text{mm}$

 Figure 5. Frequency response of car body in vertical direction.

at 0.6 Hz is found. According to the [\[9\]](#page-9-8) which studied about ride comfort of high speed train based on ISO-2631 (guide for evaluation of human exposure to whole-body vibration), the vibration of frequency range in 4 - 12 Hz for the vertical direction and 0.6 - 2 Hz for the lateral direction are sensitive to human body. Since the vibration of frequency for vertical direction is outside of the range 4 - 12 Hz, it seems that the ride comfort for vertical direction couldn't be a major concern in this case.

The frequency response of car body in lateral and rolling direction is shown in **[Figure 6](#page-7-0)**. In this case, since the peak values are found at 1.5 Hz in both cases, uncomfortability in lateral direction could be an issue, so, this value is needed to be reduced by further vibration reduction methods.

3.2. Effect of Normal Force

In this section, the effect of normal force produced in superconducting LSM propulsion control is examined. Since the typical relation between thrust and normal force in superconducting LSM control is trigonometrical with respect to the magnetic field angle as shown in **Figure** 7, the normal force with respect to the angle could be simply calculated [\[5\].](#page-9-4) In our case, due to the symmetry form in lateral direction, only vertical directional normal force is considered. By assuming that the maximum thrust force per one car is 46 kN (This value can be achieved at 90 \degree of magnetic field angle, [\[5\]\)](#page-9-4) and the slope of lateral guideway is 60 \degree , the normal forces with respect to the different magnetic field angle (*i.e.* 75˚, 80˚, 85˚, 90˚, 95˚, 100˚, 105˚) are added in right side of Equation (1) for simulation. As shown in the simulation results in **[Figure 8](#page-7-2)**, it is found that attractive normal force acts favorably to ride comfort while the repulsive force acts unfavorably. However, in both cases, these effects are negligible (*i.e.* change rates are under 1%) as summarized in **[Table 2](#page-8-0)**.

3.3. Ride Comfort Improvement Method

As reviewed in Section 3.1, the vibration frequency of lateral direction positioned within the range of 0.6 - 2 Hz is expected to influence ride comfort un-favorably. To mitigate this vibration, the electromagnetic force from the linear generator is considered. The linear generator is usually installed in high speed maglev to generate power in traveling vehicle by using the harmonic magnetic interaction with ground LSM coil. And during linear generator operation, the electromagnetic force is generated additionally from linear generator and this force could act as damper in primary suspension [\[10\].](#page-9-9) On condition that this method is also applicable to our system, the vibration reduction effect by electromagnetic force from linear generator is investigated. By assuming that the generated force with maximum value of f_m has the switched polarity according to the polarity of lateral velocity [\[10\],](#page-9-9) the electromagnetic force can be expressed like:

$$
F_m = -sign(\dot{y}_1) \cdot f_m \tag{15}
$$

To examine the effect of this force on the vehicle dynamics, Equation (15) with different value of f_m is inserted in right side of Equations (1) and (9).

Figure 7. Typical thrust and normal force as functions of the magnetic field angle [5].

The simulation results about effects of damping force from linear generator results are shown in **[Figure 9](#page-8-1)** and **[Figure 10](#page-8-2)**. As shown in figures, the ride comforts are improved effectively in both cases, and the amount of im-

Figure 9. Frequency response of vertical directional car body according to linear generator force.

provement is more remarkable in lateral and rolling direction than vertical direction. This result is summarized in **[Table 3](#page-9-10)**.

4. Conclusion

In this study, to analyze the dynamic behavior of dual-mode propulsion system which is proposed for 600 km/h

Table 3. Ride comfort improvement according to linear generator force.

level high speed, the dynamic model including guideway irregularities is established and numerical simulations are performed. From the frequency response analysis regarding ride comfort, lateral direction is expected to be more influential to ride comfort than vertical direction. And it is shown that the normal force effect on the vertical directional vehicle behavior according to the magnetic field angle would be limited even though the attractive normal force acts favorably to ride comfort. And as a ride comfort improvement method, the electromagnet force from linear generator acting as a damper is introduced and its effectiveness is confirmed.

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